# Leaving Certificate, 1888. <br> Note as to Mathematical Papers. 

## A.

The scope of the Mathematical Papers that will be set is indicated in the following list:-
No. 1. Arithmetic (I.), $1 \frac{1}{2}$ hours.-Ordinary arithmetical questions, with optional questions on logarithmic computations of an easy kind.

No. 2. Geometry and Trigonometry (I.), 2 hours.- 8 standard questions on the subject matter of Euclid, Books I., II., III., IV., VI., with easy riders and numerical examples; 4 optional questions, partly on the geometry and mensuration of solid figures, partly on modern propositions usually taught as a sequel to Euclid, on trigonometry, properties and logarithmic solution of triangles.

No. 3. Algebra and trigonometry (I.), 2 hours.-8 standard questions on algebra up to and including quadratic equations, taking in the elementary theory of irrational forms, surds, proportion, and the progressions ; 6 optional questions on the higher parts of the subject usually taught in schools, and on the elementary theory of trigonometrical functions.
No. 4. Geometrical Conics (I.), 2 hours.-8 standard questions on the parabola and the ellipse, with easy riders. 4 optional questions on the general conic, the hyperbola, and the sections of the cone.
No. 5. Analytical Geonetry (I.), 2 hours.- 8 standard questions on the straight line treated by Cartesian co-ordinates. 4 optional questions on the simpler abridged, or trilinear methods as applied to the straight line; on polar co-ordinates, the circle, and the easier parts of the conic sections.

No.6. Dynamics (I.), 2 hours.-8 standard questions on velocity, acceleration, the laws of motion, composition of forces, equilibrium, centre of gravity, the lever and its modifications, pulleys, and the inclined plane. 4 optional questions on work, energy, friction, machines in motion, and hydrostatics.
No. 7. Arithmetic (II.), $1 \frac{1}{2}$ hours.-Questions of a general kind, somewhat simpler than those set in No. 1.
No. 8. Geometry (II.), 2 hours. - 12 questions on the subject matter of Euclid, Books I., II., III., with easy riders, and possibly a question in Book IV.
No. 9. Algebra (II.), 2 hours.-12 questions on Algebra up to and including equations of 1st degree, with easy quadratics of one variable, and simple questions on greatest common measure and least common multiple.

## B.

The papers marked (I.) belong to the senior certificate, those marked (II.) to the junior certificate. Of those marked $1-6$ for the senior certificate, 1, 2, 3 are compulsory, i.e., the candidate must pass in all these to obtain the senior certificate in Mathematics. In several of these papers, the questions are divided into standard and optional. In papers 2 and 3 , a candidate can pass by doing a reasonable number of the standard questions alone. Credit will, however, be given for all questions done, and candidates desiring a certificate with honours should do as many of the optional questions as they can.

In the other senior papers, 4-6, which are not compuisory for a pass, the object of the optional questions is to give enough variety to meet the professions of the schools, and the distinction between standard and optional questions is of less importance.
C.

All the papers marked (II.) are compulsory for the junior certificate, in the sense noted above. Papers 8 and 9 will be so set that it will be possible for a candidate to pass who has not professed all the subjects mentioned: e.g., a pass in geometry may be obtained for a thorough knowledge either of Euclid I. and II., or of Euclid I. and III.

## J.

A candidate who has failed to obtain a complete senior or junior certificate may, if he desires it, obtain records of the separate subjects in which he has passed.

## E.

The use of books of mathematical tables is allowed in papers 1, 2, 3. If the school authorities do not provide books of tables, the examinees may use their own, provided they contain no manuscript notes or printed matter, other than such as is given in the introduction to Chambers' Mathematical Tables.

## F.

Should any reasonable question, regarding the terminology of the paper, for example, be asked by a candidate, the head mathematical master may answer the same publicly, provided the question asked and the answer given are recorded by the representative of the Department, and a statement of them is sent up by him along with the written papers.

## G.

On the days of examination, it should be explained to the candidates by the person superintending the examination that quality and style of work will be looked to as well as quantity; and he is requested to state very particuiariy that it is not expected that all of the large number of questions set shall be done by each candidate, the main object in setting many questions being to give a wide freedom of choice.

> Scotch Education Department,
> 31 May 1888.

## Supplementary Note as to Papers in Arithmetic and Mathematics.

Candidates for honours will take the same papers (1,2, and 3) as those for the Higher Certificate, and Honours will be awarded for special excellence in these papers. The additional papers ( 4,5 , and 6 ) can be taken by Candidates either for the Higher or Honours Grade, and the result of the examination in those papers will be specially recorded on the Certificate.

If any Candidates are to be presented in any other extra subjects not mentioned in the note dated 31st of May, special application must be made to the Department without delay. The examination in such subjects will be held on the 26th of June.

Where it is desired, a separate Certificate will be issued in Arithmetic.
Scotch Education Department,
4th June 1888.

## LEAVING CERTIFICATE, 1888.

## Examination Papers.

## ENGLISH.

I.ower Grade.

Friday, 22nd June. 10 A.m. to 12.
Ten questions only to be attempted, of which at least one must be in Section II., and ONE in Section III.

## Section I.

1. Write out and punctuate the passage read for dictation.
2. Paraphrase the following lines into correct and grammatical prose:
"Ye friends to truth, ye statesmen who survey
The rich man's joys increase, the poor's decay,

- 'Tis yours to judge how wide the limits stand

Between a splendid and a happy land.
Proud swells the tide with loads of freighted ore,
And shouting folly hails them from her shore;
Hoards, even beyond the miser's wish, abound,
And rich men flock from all the world around.
Yet count our gains. This wealth is but a name,
That leaves our useful product still the same."
3. Give some rules for grammatical analysis ; and analyse the following :
"The general reproach with which ignorance revenges the superciliousness of learning is that of pedantry; a censure which every man incurs who has at any time the misfortune to talk to those who cannot understand him, and by which the modest and timorous are sometimes frighted from the display of their acquisitions and the exertion of their powers."
4. Explain the terms : Voice, Mood and Tense ; and distinguish between weak and strong conjugations.
5. State the various formations of the plural in English, and explain the origin of each.
6. State the meaning and derivation of the suffixes in the following words : Business, Only, Orchard, Nostril, Kingdom, Worship, Every.
7. Give the derivations of the following words : Rather, Judge, School, Moralist, Victuals, Monk, Heresy, Fiction, Poet, History, Philosophy, Government, Secure, Burgh, 'Town, Sheriff, Mayor.
8. Point out any grammatical faults in the following sentences :
(a.) The savage, as well as the civilized man, recognise a divine government of the world.
(b.) In the one, nolcss than in the other, these sort of qualities are apparent.
(c.) He acted in this case like he acted in similiar cases previously.
(d.) I prefer to suffer every extremity of evil, than to yield to an order which I believe to be wrong.
(e.) The settlement of all these complicated questions, and of difficulties so threatening, demand energy as well as wisdom.
9. Give either
(1.) The plot, with a description of the characters, of any one of Shakespeare's plays.
or (2.) The plan of Chaucer's Prologue, and a description of the characters introduced.
or (3.) The scheme and occasion of Milton's Lycidas,
or (4.) A summary of the action in the earlier books of Milton's Paradise I.ost.
10. Name the principal authors in the reign either of (a) Elizabeth; (b) Charles II.; (c) Anne; (d) George III. ; or (e) Victoria.

## Section II.

11. Give an account, with dates, of the settlement of the Angles and Saxons in our country.
12. What do you understand by the Feudal System?
13. State the chief events in the reign of King John, with the leading provisions of Magna Charta.
14. Give an account of the Scottish Wars of Independence down to the Battle of Bannockburn, with dates.
15. Give some account of the causes of the Wars of the Roses, and name the chief battles in those wars.
16. Describe the progress of the Reformation down to the complete establishment of Protestantism, either in England or in Scotland.
17. State what you know of the following: The Petition of Right, Shipmoney, the Grand Remonstrance, the Self-denying Ordinance, Pride's Purge, Cromwell's Scheme of Government.
18. State the immediate causes of the Revolution of 1688.
19. Give some account of the following: The Duke of Marlborough, the Earl of Peterborough, Sir Robert Walpole, Pitt (Earl of Chatham), Edmund Burke.
20. Give some account either of the War of the Spanish Succession, or of the Seven Years' War.

## Section III.

21. Name six leading towns of England and Scotland, giving the situation, approximate population, and chief industries of each.
22. Trace, with an outline map, the course of one of the following rivers, naming the towns on its banks : the Thames, the Severn, the Humber, the Clyde, the Dee, and the Forth.
23. Name the chief mountain ranges in England and Scotland, stating the direction, and characteristic features in the formation, of each.
24. State the principal directions in which British Colonial enterprise has moved, and give the date of the establishment of our chief colonies.
25. Draw a map of British India, showing the different Presidencies and their chief towns.
26. Trace the routes to India, by the Cape of Good Hope and the Red Sea respectively, and state the most important points passed on each route.

## ENGLISH.

## Lower Grade.

Friday, 22nd June. 10 A.m,
Passage for Dictation.
The statesmen of whom we speak passed their youth surrounded by the incessant din of theological controversy. Opinions were still in a state of chaotic anarchy, intermingling, separating, advancing, receding. Sometimes the stubborn bigetry of the Conservatives seemed likely to prevail. Then the innpetuous onset of the Reformers for a moment carried all before it. Then again the resisting mass made a desperate stand, arrested the movement, and forced it slowly back. The vacillation which at that time appeared in English legislation, and which it has been the fashion to attribute to the caprice and to the power of one or two individuals, was truly a national vacillation.

## ENGLISH,

Higher Grade and First Paper for Honours Grade.
Friday, 22nd June. 10 A.m. to 12.
TEN questions only to be attempted, of which at least two mnst be in Section II. and two in Section III.

## Section I,

1. Write an Essay, of not more than three pages, on one of the following subjects:-
(1.) Party Government,
(2.) The importance of Colonial enterprise in the life of a nation.
(3.) The qualities that produce a good orator.
(4.) The influence of the invention of Printing.
2. Analyse the following, explaining the principles upon which you base your analysis :-
"High on a throne of royal state, which far
Outshone the wealth of Ormus and of Ind,
Or where the gorgeous East with richest hand

## EXAMINATION PAPERS.

Showers on her kings barbaric pearl and gold, Satan exalted sat, by merit raised
To that bad eminence."
3. Translate the following passages into modern English :-
"In a somer seson . whan soft was the sonne, I shope me in shroudes - as I a shepe were, In habite as an heremite . vnholy of workes, Went wyde in pis world • wondres to here. Ac on a May mornynge - on Maluerne hulles, Me byfel a ferly . of fairy, me thouzte; I was wery forwandred and went me to reste Vnder a brode banke - bi a bornes side, And as I lay and lened . and loked in pe wateres, I slombred in a slepyng . it sweyued so merye."
or,
The busy larke, messager of daye, Salueth in hire song the morwe graye; And fyry Phebus ryseth up so brighte, That al the orient laugheth of the lighte, And with his stremes dryeth in the greves The silver dropes, hongyng on the leeves.
And Arcite, that is in the court ryal
With Theseus, his squyer principal,
Is risen, and loketh on the merye day.
4. Comment on the words in Italics in the above passages.
5. Explain, and comment on, the following idiomatic expressionsMethinks: I was an hungred: they fell a-talking: he was done to death : many a thing : it is I : lack-a-day.
6. Compare the proportion of the Teutonic and Classical elements in modern English. At what times and through what channels has the classical element in the language chiefly been introduced ?
7. Give the derivations of the following words: prey, doom, rule battle, shire, feudal, shall, bishop, church, woman, lady, sir, madam, churl, earl.
8. Name, and give the chief works of, any two leading writers of-
(a.) Drama (excluding Shakespeare).
(b.) Epic poetry.
(c.) Satiric poetry.
9. Give some account of the life, works, and chief characteristics of any one of the following: Geoffrey Chaucer, Edmund Spenser, Ben Jonson, Jonathan Swift, John Dryden, Daniel Defoe, Dr. Samuel Johnson, William Cowper, Sir Walter Scott.

## Section II.

10. Give some account of the Danish Invasions of England, and of the settlement reached by King Alfred in the Peace of Wedmore.
11. Explain what you mean by the "Feudal System," and show how its influence has gradually failed.
12. Give some account of the work of Simon de Montfort.
13. Discuss the claims of Edward I. to the suzerainty of Scotland, and describe the war of Scottish independence to the battle of Bannockburn.
14. Give a short account of the relations between England and Scotland between 1542 and the execution of Queen Mary.
15. State the causes of the rising in Scotland against the government of Charles I., and summarise the course of affairs from the rising down to the battle of Dunbar.
16. Give the terms of the Legislative Union between England and Scotland, with some account of the negotiations which preceded it.
17. Give an account of the political career either of (1) Sir Robert Walpole, (2) the Earl of Cbatham, (3) the younger Pitt, or (4) Edmund Burke.

## Section III.

18. Trace, with an outline map, the course of one of the leading rivers in England, in Scotland, and in Ireland, naming in each case the towns upon its banks.
19. Name the leading industries of Britain, and show where the chief seats of each industry are to be found.
20. Indicate the course of the mountain ranges of Britain, and state the chief peculiarities of the geological formation of each.
21. Draw a map of the British colonies either in Africa or Australia, and state when each settlement was formed, and what are its chief resources,
22. Draw a map showing the course of the Rhine, and indicate the causes of its importance in European politics.

## ENGLISH.

HONOURS.

## Additional to the Higher Grade Paper.

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\text { Friday, 22nd June. } 2 \text { p.m. to } 5 \text { P.m. }
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1. What do you understand by the Romance languages? State and illustrate their influence upon English.
2. Classify Shakespeare's plays, either in order of time or according to subjects.
3. Distinguish between Metre, Alliteration, and Rhyme, and show how each has entered into English poetry.
4. Give the plan and purpose of the chief works either (1) of Chaucer, (2) of Spenser, (3) of Milton, or (4) of Pope, and state what in your opinion are the chief characteristics of the author you select.
5. Discuss the leading features of the literature either of the reign of Elizabeth, of that of Anne, or of that of George III. (to the end of the eighteenth century), illustrating your answer by reference to the chief authors and their works.
6. Name our principal writers of history from the days of "Clarendon to those of Macaulay.

## LATIN.

## Lower Grade.

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\text { Wednesday, 20th June. } 10 \mathrm{Am} . \text { to } 12 .
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1. Translate:

Hunt Labienus excepit, et, quum Caesaris copias despiceret, Pompeii consilium summis laudibus efferret, Noli, inquit, existimare, Pompei, hunc esse exercitum, qui Galliam Germaniamque devicerit. Omnibus interfui proeliis, neque temere incognitam rem pronuncio. Perexigua pars illius exercitus superest, magna pars deperiit: quod accidere tot proeliis fuit necesse: multos autumn pestilentia in Italia consumsit, multi domum discesserunt, multi cunt relicti in continent. An non exaudistis, ex ifs, qui per caussam valetudinis remanserunt, cohortes esse Brundisii factas? Hae copiae, quas videtis, ex delectibus horum annorum in citeriore Gallia sunt refectae, et plerique sunt ex coloniis Transpadanis: attamen, quod fuit roboris, duobus proeliis Dyrrhachins interiit. Haec quum dixisset, iuravit, se, nisi victorem, in castra non reversurum : reliquosque, ut idem facerent, hortatus est. Hoc laudans Pompeius, idem iuravit. Nee vero ex reliquis fuit quisquam, que iurare dubitaret.
(a.) Why are devicerit and dubitaret in the subjunctive mood?
(b.) Explain the case of Brundisii and roboris.
(c.) What do you understand by citeriore Gallia, and colonies Transpadanis?
2. Translate into Latin :

From them he learns that at no great distance from that place was the town of Cassivelaunus, defended by woods and marshes, whither a considerable (satis magnus) number of men and of cattle has assembled. He sets out thither with his legions ; he finds the place admirably defended by nature and artificial works (pere) ; nevertheless he proceeds (contendit) to attack it on two sides (partes). The enemy after a short delay did not stand the charge of our soldiers, and hurried off (sese ejecere) from another side of the town. A great quantity (numerus) of cattle was found, and many prisoners were taken and many men slain in the flight.
3. What cases do the following verbs govern, and how do some of them differ in meaning according to the case which follows themconvenio, consulo, invideo, plaudo, persuadeo?
4. Put into Latin:

No one is injured. One must obey the laws. There was a general departure from the town (discedo). I warn you not to do this. I warn you that the enemy is at hand.
5. Distinguish the meaning of quo, qua, quam (adverbs) ; quisquam, quisque, quisquis; liter, alio, alias, alibi.

## LATIN.

## Higher Grade.

Wednesday, 20th June. 10 A.M. to 12.

1. Translate into Latin prose:

Lucius Marcius, the Roman legate in the war against Perseus, King of Macedon, to gain time wherein to reinforce his army, set on foot some overtures of accommodation, with which the king being lulled asleep, concluded a cessation for certain days: by this means giving his enemy opportunity and leisure to repair his army, which was afterwards the occasion of his own ruin. The elder sort of Senators, notwithstanding, mindful of their forefathers' virtue, were by no means satisfied with this proceeding; but, on the contrary, condemned it as degenerating from their ancient practice, which, they said, was by valour and not by artifice, ambuscadoes, and deceitful treaties to overcome their enemies.
2. Tranlsate into English :

Fabius concione extemplo advocata obtestatus milites est ut, qua virtute rem publicam ab infestissimis hostibus defendissent, eadem se, cujus ductu auspicioque vicissent, ab impotenti crudelitate dictatoris tutarentur: venire amentem invidia iratum virtuti alienæ felicitatique, furere, quod se absente res publica egregie gesta esset, malle, si mutare fortunam posset, apud Samnites quam Romanos victoriam esse: imperium dictitare spretum, tamquam non eadem mente pugnari vetuerit qua pugnatum doleat: et tunc invidia impedire virtutem alienam voluisse cupidissimisque arma ablaturum fuisse militibus ne se absente moveri possent, et nunc id furere id ægre pati, quod sine L. Papirio non inermes non manci milites fuerint, quod se Q. Fabius magistrum equitum duxerit ac non accensum dictatoris. Quid illum facturum fuisse, si, quod belli casus ferunt Marsque communis, adversa pugna evenisset, qui sibi devictis hostibus re publica bene gesta ita ut non ab illo unico duce melius geri potuerit-supplicium magistro equitum minetur ! neque illum magistro equitun infestiorem quam tribunis militum quam centurionibus quam militibus esse.

## Grammatical Questions.

1. Explain, and illustrate by examples, the force and uses of the ethical dative, the predicative dative, the complementary infinitive (after verbs and adjectives) the infinitive of surprise or indignation, the historical infinitive.
2. Point out the changes, in the passage set for translation, required to turn the oratio obliqua into oratio directa.
3. Point out and comment on irregularities of construction in the following :-

Quid tibi sum auctor?-medendis corporibus-cum equidem invideor.-Non te haec pudent ?- Eternas quoniam poenas in morte timendum est-Carmina quae scribuntur aquae potoribus.

## LATIN.

## Honours.

First Paper.
Wednesday, 20th June. 10 A.M. to 1 p.m.
Translate-

1. Est procul in pelago saxum spumantia contra litora, quod tumidis submersum tunditur olim fluctibus, hiberni condunt ubi sidera Cori; tranquillo silet immotaque attollitur unda rampus et apricis statio gratissima mergis. Hic viridem Aeneas frondenti ex ilice metam constituit signum nautis pater, unde reverti scirent et longos ubi circumflectere cursus. Tum loca sorte legunt, ipsique in puppibus auro ductores longe effulgent ostroque decori; cetera populea velatur fronde iuventus nudatosque umeros oleo perfusa nitescit. Considunt transtris, intentaque bracchia remis ; intenti exspectant signum, exsultantiaque haurit corda pavor pulsans laudumque arrecta cupido. Inde ubi clara dedit sonitum tuba, finibus omnes, haud mora, prosiluere suis: ferit aethera clamor nauticus, adductis spumant freta versa lacertis. Infindunt pariter sulcos, totumque dehiscit convulsum remis rostrisque tridentibus aequor.
2. Quintius fuit P. Quintii huius frater, sane ceterarum rerum paterfamilias et prudens et attentus, una in re paullo minus consideratus, qui societatem cum Sex. Naevio fecerit, viro bono, verumtamen non ita instituto, ut iura societatis et officia certi patrisfamilias nosse posset : non quo ei deesset ingenium : nam neque parum facetus scurra Sex. Naevius, neque inhumanus praeco est umquam existimatus. Quid ergo est? Quum ei natura nihil melius, quam vocem dedisset, pater nihil praeter libertatem reliquisset, vocem in quaestum contulit; libertate usus est, quo impunius dicax esset. Quare quod socium tibi eum velles adiungere, nihil erat, nisi ut in tua pecunia condisceret, qui pecuniae fructus esset. Tamen inductus consuetudine ac familiaritate Quintius fecit, ut dixi, societatem earum rerum, quae in Grallia comparabantur. Erat ei pecuaria res ampla et rustica sane bene culta et fructuosa. Tollitur ab atriis Liciniis atque a praeconum consessu in Galliam Naevius, et trans Alpes usque transfertur. Fit magna mutatio loci, non ingenii. Nam, qui ab adolescentulo quarstum sibi instituisset sine impendio, posteaquam nescio quid impendit et in commune contulit, mediocri quaestu coutentus esse nov poterat. Nec mirum, si is, qui vocem venalem habuerat, ea, quae voce quaesierat, magno sibi quaestui fore putabat. Itaque hercule haud mediocriter de communi quidquid poterat ad se in privatain donum sevocabat.
3. Ea tempestate Cassius ceteros praeminebat peritia legum: nam militares artes per otium ignotae, industriosque aut ignavos pax iu aequo tenet. Ac tamen quantum sine bello dabatur, revocare priscum morem, exercitare legiones, cura provisu perinde agere
ac si hostis ingrueret; ita dignum maioribus suis et familia Cassia ratus per illas quoque gentes celebrata. Igitur excitis quorum de sententia petitus rex, positisque castris apud Zeugma, unde maxime pervius amnis, postquam inlustres Parthi rexque Arabum Acbarus advenerat, monet Meherdaten, barbarorum impetus acres cunctatione languescere aut in perfidiam mutari : ita urgueret coepta. Quod spretum fraude Acbari, qui iuvenem ignarum et summam fortunam in luxu ratum multos per dies attinuit apud oppidum Edessam. Et vocante Carene promptasque res ostentante, si citi advenissent, non comıninus Mesopotamiam, sed flexu Armenianı petunt, id temporis inportunam, quia hiems occipiebat,
4. Quinque satis fuerant; nam sex septemve libelli est nimium : quid adhuc ludere, Musa, iurat ?
Sit pudor, et finis. Iam plus nihil addere nobis fama potest : teritur noster ubique liber :
et cunı rupta situ Messallae saxa iacebunt, altaque cum Licini marmora pulvis erunt,
me tamen ora legent, et secum pluriuus hospes ad patrias sedes carmina nostra feret.
Finieram, cum sic respondit nona sororum, cui coma et unguento sordida vestis erat:
Tune potes dulces, ingrate, relinquere nugas? Dic mihi, quid melius desidiosus ages?
An iuvat ad tragicos soccum transferre cothurnos? aspera vel paribus bella tonare modis,
praelegat ut tumidus rauca te voce magister, oderit et grandis virgo bonusque puer ?
Scribant ista graves nimium, nimiumque severi, quos media miseros nocte lucerna videt.
At tu Romano lepidos sale tinge libellos; agnoscat mores vita legat que suos.
Angusta cantare licet videaris avena, dum tua multorum vincat avena tukas.

## LATIN.

Honours.
Second Paper.
Wednesday, 20th June, 2 p.м. to 5 p.м.

1. Translate into Latin prose :-

Never was any commander more beloved. He governed men by their reason and their affection; they knew that he was incapable of caprice or tyranny, and they obeyed him with alacrity and joy, because he possessed their confidence as well as their love. "Our Nel.," they used to say, "is as brave as a lion, " and as gentle as a lamb." Severe discipline he detested, though he had been bred in a severe school ; he never inflicted corporal punishment if it were possible to avoid it, and, when compelled to euforce it, he, who was familiar with wounds and death, suffered like a woman. In his whole life Nelson was never known to act unkindly to an officer. If he was asked to
prosecute one for ill behaviour, he used to answer : "that there " was no occasion for him to ruin a poor fellow, who was " sufficiently his own enemy to ruin himself." But in Nelson there was more than the easiness and humanity of a happy nature ; he did not merely abstain from injury; his was an active and watchful benevolence, ever desirous not only to render justice, but to do good.

## General Questions.

1. Discuss briefly the chief differences between English and Latin prose style, in regard to (1) the arrangement and connexion of words and clauses in a sentence, and of sentences in a continuous passage ; (2) the use of abstract and concrete, and of metaphorical and figurative, modes of expression.
2. Write, with dates, a short life of (1) Horace, or (2) Cicero, supporting and illustrating your remarks by reference to, or quotation from, their own works.
3. Distinguish between patricii and nobiles, gens and familia, nomen, cognomen and agnomen. Mention and distinguish some of the more eminent patrician and plebeian noble houses and families, and of the more illustrions individuals belonging to them, in the last century of the Republic.

## GREEK.

## Lower Grade,

$$
\text { Thursday, 21st June. } 10 \text { A.m. to } 12 .
$$

1. Translate:

 eivas סuráuevoc.

 ditayaбias.





 बivà ทีкєи!;




Give the 1st pers. sing. of the fut. indic., perf. indic. act., and aor.


III. Translate into Greek :
(1.) When will you come to me at my house ?
(2.) Do not write to me until you hear.
(3.) The quicker ( $\tau a x{ }^{\text {b }}$, quick) you go away the quicker you will return (àyéyas).
(4.) Late ( $\stackrel{\alpha}{ } \psi^{\prime}$ ) in the day he led out his army.
(5.) I think that if they are ruined ( $\delta \Delta x \phi \theta \epsilon i p \epsilon i y)$ no one will succour ( $\operatorname{\beta an} \theta \theta$ eiv $)$ us.

## GREEK.

## Higher Grade.

Thursday, 21 st June, 10 A.m. to 12.
I. Translate:-















II. Translate into Greek :-
(1.) I wish to speak before I die.
(2.) So perish all who do such things !
(3.) He knew that he was wiser than any of his contemporaries.
(4.) Whenever he asked the question, What is Virtue? he got no clear answer.
(5.) Do you not think that they knew who you were?
(6.) All through his life he strove to serve his country.
III. Correct the Greek of the following sentences :-




Define " stem," " verb-stem," " tense-stem."
 of $\beta \lambda \alpha \beta-, \tau \alpha \phi-,{ }_{e}^{\epsilon} \pi \pi i \delta-, \tau \rho a \pi-$

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## GREEK.

## Honours.

First Paper.
Thursday, 21 st June. 10 A.M. to 1 p.m.
I Translate:-















 ขขั้ катทүораั้ аข่тои̃.





























r.
(1.) What are the chief points of difference between a Greek $\pi j^{\prime} \lambda_{s}$ and a modern State? Illustrate the relations of a Greek colony to the mother country.
(2.) What were the functions (i) of the $\beta$ ovin'y (ii) of the Areopagus at Athens?

## GREEK.

Honours.
Second Paper.
Thursday, 21st June. 2 p.M. to 5 P.M.
I. For Greek prose:-

This letter somewhat disconcerted Elizabeth's plan, but did not divert her from the prosecution of it. She laid the matter before the privy council, and it was there determined, notwithstanding the entreaties and remonstrances of the Scottish queen, to go on with the inquiry into her conduct; and until that were finished, it was agreed that Elizabeth could not, consistently with her own honour, or with the safety of her government, either give the assistance which she demanded, or permit her to retire out of the kingdom. Lest she should have an opportunity of escaping, while she resided so near Scotland, it was thought advisable to remove her to some place at a greater distance from the borders.

## Robertson.

II. Distinguish between Attic and Homeric usage in regard to (1) prepositions, (2) the subjunctive mood, (3) conditional sentences.
III. Trace historically the meaning of the words $\delta \tilde{\eta} \mu 05$, $\delta i \kappa \eta, \tau \mu \gamma^{\prime}$,


## FRENCH.

## Lower Grade,

Tuesday, 19th June. 10 A.m. to 12.

1. Translate into English :-

Le prince ${ }^{1}$ Eugène conserva ${ }^{2}$ toujours sa supériorité sur le maréchal de Villeroi. Enfin, au cceur de l'hiver, un jour que ce maréchal dormait ${ }^{3}$ avec sécurité dans Crémone, ville ${ }^{4}$ assez forte, et munie d'une très grande garnison, il est réveillé au bruit des
décharges de mousqueterie. Il se lève ${ }^{5}$ en toute hâte, monte à cheval ; la première chose qu'il rencontre ${ }^{6}$, c'est un escadron ennemi. Le maréchal aussitôt est fait prisonnier ${ }^{7}$ et conduit hors de la ville, sans savoir ${ }^{8}$ ce qui s'y passait, et sans pouvoir ${ }^{8}$ imaginer la cause d'un événement si étrange. Le prince Engène était déjà à Crémone. Un prêtre ${ }^{9}$, nommé Bozzoli, avait introduit ${ }^{10}$ les troupes allemandes ${ }^{11}$ par un égout (gutter, drain). Quatre cents ${ }^{12}$ soldate, entrés par cet égout dans la maison du prêtre, avaient sur-le-champ égorgé la garde des deux portes; les deux portes ouvertes ${ }^{13}$, le prince Eugène entre avec qquatre mille ${ }^{14}$ hommes. Tout cela s'était fait avant que le gouverneur, qui était Espagnol, s'en fût douté ${ }^{15}$, et avant que ${ }^{16}$ le maréchal de Villeroi fût éveillé. Le secret, l'ordre, la diligence, toutes les précautions possibles avaient préparé l'entreprise.

## Voltaire.

2. Grammatical questions on the above passage :-
(1.) Give feminine of this. (2.) 3rd sing. and 3rd plur. imperfect subj. (3.) 3rd sing, present, preterite (or past) definite, and future. (4.) Why not une ville? (5.) 3rd plur. present, preterite definite, preterite indefinite, and future of se lever. (6.) Put this in the preterite indefinite (-'which he has'...). (7.) Turn "est fait prisonnier" into the feminine. (8.) 3rd sing. and plur. present, preterite definite and future of savoir and pouvoir. (9.) Feminine of prêtre. (10.) 3rd plur. present and imperfect subjunctive. (11.) Give name of country in French. (12.) Give rule regarding this sign of plural. (13.) 1st sing. and plur. present and preterite definite indicative. (14.) Why not milles? When does it take the s? (15.) Give the negative form and the ferninine of il s'en fût douté; also the plural of both. (16.) Give three other conjunctions which require the subjunctive.
3. Translate into French :-

In 1356 the Black Prince won a glorious victory near Poitiers. He had only twelve thousand men, while the French had sixty thousand. John, the King of France, fell into the hands of the English knights. The prince treated him with the greatest politeness, and sent him to London. During his sojourn in England he was shown (trsl. one showed him) all the respect due to a crowned head. At last having renounced the portion of his country which Edward had conquered, he was set at (en) liberty. Before setting out for France, he promised, however, to send a large sum of gold as ransom (rançon). But when he found that his subjects could not raise this money he returned te England, and died there.

## FRENCH.

## Higher Gradr.

Tuesday, 19th Juиe. 10 A.m. to 12.

1. Translate into English :-
a. Au milieu de ces petitesses et de cette corruption parut à la cour de France une figure gigantesque, et que semblait grandir
encore son aspect à demi barbare: c'était Pierre le Grand, le créateur de la Russie. Il y fut reçu avec magnificence et les plus délicates attentions, mais ne se laissa point séduire par ces brillants dehors. Pierre premier ne pouvait, on le pense bien, se plier à toutes les règles de l'étiquette. Quand on lui présenta le jeune roi, il l'enleva de terre et l'embrassa sur les deux joues à la grande stupéfaction des seigneurs. Il lui fallut de la bière dans sa loge à l'Opéra. Ce fut le régent lui-même qui lui offrit le verre et la serviette. Aux Invalides,* il goûta la soupe des soldats, but à leur santé, leur frappant sur l'épaule et les appelant camarades. Il vit à la Sorbonne $\dagger$ la statue de Richelieu sculptée par Girardon, et saisissant ce marbre dans ses bras: "Grand homme," s'ćcria-t-il, " je t'aurais donné la moitié de mes Etats "pour apprendre de toi à gouverner l'antre!" Ainsi tout ce qu'il trouva à admirer ici, ce fut le passé; le reste lui sembla si pauvre qu'il annonça la décadence et la ruine prochaine du peuple français. Il ne l'avait vu qu'à la surface, et le jugeait d'après la cour. Mais pour celle-ci il avait prédit juste, noblesse et royauté se mouraient.
V. Duruy.
b. Infâme paresseux ! tu ne veux donc ríen faire ?

Dit un jour un maître en colère
$\AA$ À son valet sous un arbre endormi.
Au lieu de travailler, dormir en plein midi!
Tu ne mérites pas que le soleil t'éclaire.
Vous avez bien raison, ma foi,
Dit le dormeur, et mes torts sont sans nombre ;
Le soleil n'est pas fait pour moi :
Voilà pourquoi je me suis mis à I'ombre.
II. Translate into French :-

It was at a supper with Prince Menzikoff that the Emperor saw Catherine for the first time, and fell in love with (trsl. became amorous of) her : he married her secretly in 1\%07, not charmed by female artifices, but because he found in her a firmness of soul capable of seconding his undertakings, and even of continuing them after him. He had already repudiated long since his first wife Ottokefa, a boyard's daughter, who was accused of opposing the changes which he made in his dominions. This crime was the greatest in the eyes of the Czar ; he would have in his family only persons who thought as he (did). He believed he discerned in this foreign slave the qualities of a sovereign, though she had none of the virtues of her sex. For her sake he disdained the prejudices which would have restrained an ordiuary man : he caused (trsl. by faire) her to be crowned Empress. The same talents which made her the wife of Peter Alexiowitz, gave her the empire after the death of her husband. Europe has beheld with surprise this woman, who could neither read nor write, repairing her education and her weaknesses by her courage, and filling with glory the throne of a legislator.

Voltaire.

* Les Invalides, the Paris hospital for disabled soldiers.
$\dagger$ La Sorbonne, a building containing part of the Paris University.
(1.) Give the plural and meaning of : quel nouveau détail, son bel ail, ce ciel bleu, celui du monsieur, madame votre grand'mère.
(2.) Give the feminine and meaning of un prince étranger, ce gros paysan, mon neveu hui-même, plusieurs lions furieur, tous leurs fils.
(3.) Distinguish between :-des, dès, dés ; plutôt, plus tôt ; mur, mûr; la tache, la tâche ; il vit, il vît.
(4.) a. Third singular and plural present and preterite (or past) definite indicative of: decevoir, paraitre, prevoir, s'en aller, pouvoir.
b. Second singular and plural preterite (or past) definite, future, and imperative of : voir, savoir, écrire, s'asseoir, s'en aller.
c. Third singular and plural pluperfect of se fâcher (mascu: line and feminine), (1) negatively, (2) interrogatively.
(5.) Give the French for :-(a) I have just dined ; (b) I am about to go ; (c) You ought to go ; (d) I doubt that this is true; (e) I fear he will come.


## FRENCH.

## Honours.

Tuesday, 19th June. 10 A.sm. to 1 p,y.
Translate into English :-
(a.) On avait besoin d'un grand génie pour corriger les fautes de politique qu'on n'avait cessé de commettre. Il existait, ce puissant génie, dans la persoune du favori de la reine mère, Richelieu évêque de Luçon, dont nous avons déjà parlé, et à qui il était réservé de changer la face de l' ${ }^{\text {Europe. On verra bientôt }}$ ce prélat ambitieux maitriser un monarque faible, soumettre la noblesse au joug des lois et de sq volonté, et ne pas regarder au mal qu'il lui faudra faire à la France pour parvenir à l'accomplissement de ses vues. La reine mère, depuis sa réconciliation avec son fils, était rentrée au conseil, et désirait d'y introduire Richelieu, qui, d'abord créature de Concini, était ensuite devenu cardinal par l'entremise de De Laynes. Il forg̣a bientôt tous les obstacles qui arrêtaient sa fortune; car les ministres craignant son ambition, et surtout lạ supériorité de ses lumières, l'avaient décrié dans l'esprit de Louis. Les galanteries dont on l'accusait ne pouvaient manquer de choquer ce prince dévot, trop soupçonneux d'ailleurs, et trop jaloux de l'autorité, pour ne pas craindre celui qu'on peignait comme le plus ambitieux des courtisans. Marie de Médicis ne se rebuta point; elle parvint à faire disgracier les ennemis du cardinal, qui, à leur grande mortification, fut enfin admis au ministère en 1624 . Plus il désirait cette place, plus il affecta de répugnance à l'accepter. Sa mauvaise santé, disait-il, le rendait incapable d'un long travail; tout ce qu'il pouvait faire, était d'assister au conseil de temps en temps, sans ge mêler d'aqfaires d'Etat.
(b.) Au bout de quinze jours nous étions sans un sou J'avais passé ce temps à marcher comme un fou Seul, allant devant moi, tout droit, parmi la foule. Car le bruit des cités vous endort et vous soûle, Et, mieux que l'alcool, fait oublier la faim. Mais, comme je rentrais, une fois, vers la fin D'une après-midi froide et grise de décembre, Je vis ma femme assive en un coin de la chambre, Avec les deux petits serrés contre son sein; Et je pensais : "C'est moi qui suis leur assassin !" Quand la vieille me dit, douce et presque confuse: "Mon pauvre homme, le Mont-de Piété refuse Le dernier matelas, comme étant trop 'mauvais, Où vas-tu maintenant trouver du pain ?"-" $J$ 'y vais," Répondis-je, et, prenant à deux mains mon courage, Je résolus d'aller me remettre à l'ouvrage.

> François Coprée, "La grève des forgerons."
II. Translate into French :-

As she uttered these words, she went to take the candle from the table; she ran over all the rooms, one after the other, and saw there neither her maids nor her sister; she even observed that they had carried off all their clothes. Her suspicions now appeared to her but too well founded; she came to me, and said to me with much emotion, "Perfidious man, add not dissimula" tion to treachery! It was by no means chance that caused thee "to come in here: thou art one of Don Fernando's suite, and hast "a share in his crime. But do not hope to escape : people enough "still remain to me to seize thee." "Madam," I answered, " do "not confound me with your enemies! I do not at all know Don "Fernando ; I do not even know who you are. I am an unfor"tunate man whom an affair of honour obliges to leave Madrid;
" and I swear, by all that is sacred, that, but for ( $\operatorname{trsl}$. ., without)
" the storm which surprised me, I would not have entered your
" house! Judge, therefore, more favourably of me: instead of " believing me an accomplice (complice) in the crime which offends "you, think me rather disposed to revenge you!" These last words, and the tone in which I pronounced them, appeased the lady, who seemed to look upon me no longer as her enemy; but if she lost her anger, it was only to give herself up to her grief.

Le Sage.
III.-

1. Give the plural and meaning of chef-lieu, chef-d'ouvre, chou-fleur, tire-bouchon, passe-partout, gentilhomme, arc-en-ciel, franctireur, pince-nez.
2. State the rule regarding the treatment of adjectives qualifying the noun gens, illustrating it by the following examples:- $a$, these good people are tiresome (ennuyeux) ; $b$, all old people; $c$, all black people; $d$, all honest people; $e$, these people are all very happy.
3. Exemplify the adverbial use of tout, by making each of the following sentences-
il était tout prêt;
il fut tout étonné ;
tout heureux qu'il est ;
tout honteux qu'il était-
$a$. plural ; b. feminine singular; c. feminine plural.
4. Distinguish between:-
le mémoire-la mémoire.
un brave homme-un homme brave.
je n'en veux plus-je ne lui en veux plus.
il me tarde de la voir-il ne tardera pas à la voir.
ils ne font que sortir-ils ne font que de sortir.
5. Show by one or two examples what tenses (and moods) are used in conditional clauses with si.
6. Give the English, or French, equivalents of any three of each of the following two sets of idiomatic phrases:-
a. nous l'avons échappé belle.
b. il riait sous cape.
$c_{\text {: }}$ il gagne à être connu.
d. il se mettrait en quatre pour moi.
$e$. en venir aux mains.
$a$. no sooner said than done.
$b$. to make one's self at home.
c. we heard from him yesterday.
$d$. it is not worth while.
$e_{i}$ I cannot help it.

## GERMAN.

## Lower Grade.

Tuesday, 19th June. 2 PM, to 4 P.M.
I. Translate into English:-

Sur Seit Mexanbergి begి (brofen lebte in Sorintly ein fejr merf= mürbiger Mann, namensิ Diogeness. Der mollte zeigen, mie wenig ber Wenid beburfe, um glưflidy zu leben; er ging in einem zerrififenten

 ber Goglen seand trinfen faty. NHexanber, ber bon igm gefort gatte, fam $z^{4}$ ifnt. Er $\operatorname{lag}$ gerabe vor feiner Tonne, um fidi an ber Sonne zu
 nabler $z^{4}$ betraften. Stexanber rebete lange mit ifm und fand feine

 ein menig auß̧ ber ©onne!" Die Begleiter beş ©önigę murben zornig üfer biefe Beradtung feiner ©nabe. WIexanber aber fprady: "Wienn


After Э. ๔. Mnbră.
II. Translate into German :-

Mary, have you seen my brother ?-Yes, Miss, he is in the garden. What is he doing there?-He is playing with another boy. Tell him he must come in. It is five o'clock. He has to work now. Here he comes already. Where is your (translate thy) friend, Charies ?-He has gone home. Who was it?-It was Henry, the son of our neighbour, Is he pat much older than you (translate thou)?-Only one year ; and $b$ is not quite so tall as I.
(1.) Give the German words-in the nominative and genitive singular, and nominative plural, with the definite articleof any ten of the following:-house, dog, book, flower, woman, letter, hand, stick, ship, roof, pen, star, town, country, king.
(2.) Decline (singular and plural) : biefer ßaum; and the third personal pronoun.
(3.) Write out the cardinal numbers from 1 to 20 ; and the ordinals from 1st to 5 th.
(4.) Give the third person singular present, imperfect, and perfect indicative active of:-finben, feben, effen, fagen, fiprecten, fafreiben, miffert, fönnen.
(5.) Write out the perfect indicative active of geffen; and the present indicative passive of loben.

## GERMAN.

## Higher Grade.

Tuesday, 19th June. 2 p.m. to 4 P.m.
I. Translate into English :-
a. گriebrid $\mathfrak{B a r b a r o f i a ~ w a r ~ e i n ~ u n d ~ b r e i f i g ~ S a j r e ~ a l t , ~ a l 8 ~ e x ~ b e n ~}$ Thron beftieg (1152). Su jener Seit gab eş in Deutioland §5aber uno Smiefpalt genug. Die Fürfen fritten unter einanber unb berlangten bou Saifer, er folle regierent, wie ez ifnen gefiele. Da befobloñ bab siaifertum wieber fitarf zu macjen, unt reidy an Madit unb (5yren, mie ez zu fiarle beg ©rojen Seit gewefen war. Die Naubritter am Rbein liej er feinen. 2 rm fütilen. Gedfis und fedfig ifrer Burgent Iegte er in Trümmer unb fajaffte Flutje uno Cidjerbeit im beutidien §eid. Unbeftritten mar er bas kaupt ber ganzen © ofriftengeit, (5efanote aus affen dänbern Europas Gulbigten igm im Namen ifirer Fưften. Segen bie Lpmbarbifden Gtäbte Norbitaliens, bie feine Dberfobeit lange nidgt anerfennen wollten, unternabm or fünf Siriegs. züge; unt befonbers bie Ctabt Mailand mupte für igren Trode und

 pourbe er überalf mit §reube unb Subel empfangen.
b. E®8 mar im Dorje §octzeit,

Die (3afte fdimaffen unb jprangen;
Da fam zu $^{1}$ bem frolyen Fefte
2tud ein alter © ${ }^{2}$ inger gegangen.
§ei! mag̉ man bem jungen ફaare
Für reidge (ऊefajenfe befdieb!
Der Sanger bradte zum Fefle
nidats als cin fleintes Rieb.
Das 5odzzeitzpaar unb bie cbafte
Sinb lảngit im Grabe verbratt, Berwittert find alle ©jefuente; Das \&ied left immer nody fort:
II. Translate into German :-

One of the knights rode one day too far from the camp, and lost his way: He got (translate came) into a great wood, and feared he might meet a band of enemies. At last he saw a young herdsman (Sift) who sat under a tree; and he said, "My boy,
" I will give thee this horse, if thou wilt lead me back to my
" friends." The lad replied, "It is too late now. Come home
" with me, and I will go with you as your guide to-morrow
" morning." The knight went with the boy, and slept the whole night in his father's hut. Next day he was led back to the camp. The youth, whose name was Godwin, remained with him. He was clever and brave, and rose (Iteigen) afterwards to high rank at the Danish court.
III.-
(1.) Give the German words-in the nominative and genitive singular, and nominative plural, with the definite articleof any ten of the following:-people, week, month, virtue, pain, disease, heart, eye, quality, art, pleasure, castle, passion, prince, sea.
(2.) Decline (singular and plural):-mein gater Freunb, and (singular) תaifer karl per (Grope.
(3.) Distinguish between :Der Şeibe, Die Saibe; bur See, Die See ; Der Werbienti, DaB

(4.) Give the third singular present, imperfect, and perfect indicative active (with the meanings) of : Gefarten, antelymen, meggeffen, zerbredfen, bejefien, berlieren, lenten, fönten.
(5.) Translate:-
a. I know that you know him.
b. A man came running.
c. It is half-past seven o'clock.
(6.) State what cases are governed by the prepositions: Wei, wegent, burctif ; giving one example for each.

GERMAN.
Honours.
Tuesday, 19th June. 2 p.m. to 5 p.m.

1. Translate into English :-
a. Etna wei binate nad Der Surüuffunft Marls au Nom öffnete Favia fm die Shore. Die Stabs Kate maftenb Der langer Befagerung biel gefitten bur Sranffeit un angel ; Die §ranfen abe madden notch timer cine grope Bette, ut karl überliej biffetbe gean feinen
 Der einft fen Sambiegersolfn gewefen war, gefangen überlifert, melt
 fütren. Deftberiug ward, woe es Geip̆t, in in תitpfer geftecft, roo er fin Refer alB Mind enbigte. Dab Safiefal finer Bemaflin if gärflid unbefannt. Seiner Totter Deftberata, die pint farl
 oas Ser dijon gebrodjen bor biefen $\mathfrak{T}$ gen der Trubfat. Spin Sofia

2toalgiz batte fith in Werona tapfer berteibigt; alz aber Pavia gefallen
 fein Scficifal voraugfeben. Demjelfent zu entgeben, entzalo
 Bifa nady תomptantinopel, mo er eine gaffireumblide Sufnatme fanb.

> 5. \&uben, "(sefduidfte bezి Deutiden Borfz."
b. Znei ๔eelen molnnen, acd! in meiner Bruft,

Die eine will fitif bon ber anbern tremen;
Die cint gialt, in berber \&tebestuft,
(Cith an bie $\mathfrak{W B e l t}$, mit flammernben Deganen;
Die arbre beft genarttjam fidid yom Duft
Su ben (befilben yober 2lynen.
D, gieft es ©eifer in ber Nuft,
Die zmifden "Ero' unt §imuel ferrident meben, -
So fleiget nieber aus ben golonen Duft
Uno futhrt midh meg, zu neuem buntem seben!
Sa, wäre nur ein Zaubermantel mein,
Utio trüg' or midf in frembe \&änber,
Wir follt' er um die fioftlidfiten Gemolnber,
nidut fril um einen Rōnigantantel fein!
II. Translate into German :-

The Swede Gustavus Wasa was persecuted by King Christian the Second of Denmark, because he opposed the Danish rule, He therefore fled, disguised as a peasant, to the Dalecarlian mines, where he was for a long time sheltered from his pursuers, One day, however, his stay at a farm-house had been betrayed to the Danes. The farmer put him at once on a cart (waggon) filled with straw, and drove him to the nearest village. On the way he was stopped by Danish horsemen, who searched the cart, and pierced the straw with their swords in all directions. Thereby Gustavus was wounded in the leg; but he remained lying quiet, and did not betray himself by a sound. When the peasant saw that the blood from the wound was trickling through the cart upon the snow, he quickly cut one of the two horses in the leg, in order that the soldiers should think that the blood came from the poor beast. Thus he arrived safely in the village, where he handed over his protégé (ऽđübling) to some friends.

## III.-

(1.) Decline the German of "His Majesty King William of Prussia."
(2.) Form abstract nouns (with definite article, and meaning) from any eight of the following adjectives :-gut, fromm, fanft, jung, gefund, reiff, 耳ei ${ }^{2}$, , bod tapfer, Iant, frei, werth.
(3.) Give five adjectives (with meanings) that govern the genitive, and five that govern the dative.
(4.) Give the meaning of any eight of the following reflective verbs, and state what prepositions are required after them:-fidd munbern, ficid fürditen, fict berlafien, fid befinnen
 :pöynen, fid fügen, fidi begeiftern, fidid ridften.
(5.) State the cases in which the past participle is used in German :- $a$. instead of the present participle; $b$. instead of the infinitive.
(6.) Give the English or German equivalents of any three of each of the following two sets of idiomatic phrases :-
a. mit dem plauen \{luge babonfommen.
b. aus frein Gtüuforn.
c. fo mic fo.
d. ain gefurbentes $\mathfrak{F r e f f e r}$.
e. cinema cine $\mathfrak{S}_{3 \text { fin }}$ pricier.
a. And so forth.
b. Now and then.
c. As far as I know.
d. I could not help it.
e. For my sake.

No. 7.-ARITHMETIC (II.).
Lower Grade,
Monilay, 18 th June. 10 A.M. to 11.30 A.M.
Give your working in full.
Endeavour rather to answer a moderate number of Questions accurately and fully than to answer a large number imperfectly.

1. Explain the rule for the addition of vulgar fractions.

$$
\text { Simplify } \frac{6756}{6193}-\frac{4114}{4488^{\circ}}
$$

2. Find the total of the following bill :-

3. Express as a single decimal

$$
3 \cdot 164 \times 2 \cdot 013+\cdot 0163 \div \cdot 0084-1 \cdot 305 \times 2 \cdot 006
$$

4. Calculate the simple interest on $£ 3,4684 s .6 \mathrm{~d}$. for $4 \cdot 25$ years at $3 \cdot 168$ per cent.
5. A grocer sells his best quality of tea at $3 s .6 d$. per lb., and thereby gains a profit of 4 per cent. ; he sells his second quality at $2 s .6 d$ per lb ., gaining a profit of 6 per cent. At what prices must he sell a mixture composed of two parts of the second quality to one of the first, so as to gain a profit of 5 per cent.?
6. A wall is covered with plaster $1 \frac{1}{4}$ inches thick; how many square yards will be covered by a cubic yard of plaster ?
7. Which is the greatest of the three sums $\frac{1}{19}$ of $£ 1$, $\frac{1}{20}$ of a guinea, $\frac{7}{18}$ of half-a-crown ?
8. Express
(1.) 17294544 square inches in acres, and
(2.) $2 \frac{1}{2}$ lbs. troy, in lbs., oz., drs. avoirdupois, 7,000 grains going to an avoirdupois lb ., and 5,760 grains to a troy lb.
9. One man can do a piece of work in 12 hours, another in 16 , another in 48. How long would all three working together take to finish it?
10. If $£ 1,095$ lying at interest for 117 days becomes $£ 1,1188$ s., what is the rate of interest per cent. per annum ?
11. A person owning $£ 1,0003$ per cent. stock, has to sell out as much as will pay a debt of $£ 10515$ s. If the 3 per cents, are at 94 , how much stock has he to sell out?
12. Simplify $\frac{2 \cdot 03+1 \cdot 21}{2 \cdot 03-1 \cdot 21}$, giving the answer in decimals.

Reduce every term in this to a fraction, and compare the results.

> No. 1.-ARITHMETIC (I.).

## Higher Grade and Honours.

Monday, 18th June. 10 A.M. to 11.30 A.m.
Give your working in full.
Endeavour rather to answer a moderate number of Questions accurately and fully than to answer a large number imperfectly.

1. Explain the principle of the process for converting a vulgar into a decimal fraction ; and indicate the conditions that the decimal terminate.
Express-

$$
\frac{\left(\frac{3}{4}+\frac{1}{8}-\frac{1}{2}\right)\left(\frac{3}{4}+\frac{1}{8}+\frac{1}{2}\right)+\left(1-\frac{3}{4}-\frac{1}{8}\right)\left(1+\frac{3}{4}+\frac{1}{8}\right)}{\frac{7}{22}\left(\frac{1}{2}+\frac{3}{8}\right)}
$$

as a decimal (to 4 places).
2. Express in English money to the nearest penny the amount of the following bill in French money:-3.35 articles, at 6.37 fr.; 23.63 articles, at 1.34 fr .; $15 \cdot 37$ articles, at $7 \cdot 15 \mathrm{fr}$. ; allowing $25 \cdot 42 \mathrm{fr}$. for $£ 1$.
3. A certain sum of money put out at $4 \frac{1}{2}$ per cent., simple interest, for 10 years, amounted to $£ 1,356$ after income tax was deducted from the interest at the rate of $5 d$. in the pound. What was the sum ?
4. I bought 25 shares of a certain Company for $£ 135$ each, the paidup capital for each share being $£ 100$. During the year I got a dividend of $5 \frac{1}{2}$ per cent. on the paid-up capital, and a bonus of $£ 35$ on my 25 shares. What rate of interest did my investment bring me?
5 . For how much should a house, worth $£ 5,122$, be insured at $2 \frac{1}{2}$ per cent. so that in case of loss the value of the house and the insurance premium may be repaid?
6. What is the difference between simple interest and true discount on a bill for $£ 400$ due in 9 months, when interest is at 4 per cent. per annum?
7. A locomotive engine making 162 strokes per minute, travels 90 miles in two hours; how many strokes per minute must the same engine make to do 200 miles in $4 \frac{1}{2}$ hours ?
8. From 9.6 of a $£$ take 5.037 of a guinea, and express the result in decimals of a shilling.

## Optional Questions.

(In these Questions the Candidate may use Logarithms.)
9. The population of a country was $4,314,000$ to begin with, and increased by 3.168 per cent. every year for 5 years. What was the population at the end of the 5 years?
10. A square pond is surrounded by a strip of lawn whose breadth is the same on all the four sides. If the side of the pond be 32 yds .2 ft ., and the breadth of the lawn 25 yds .1 ft ., find the area of the lawn.
11. An estate, which consists of a circular piece of ground $1 \frac{1}{4}$ miles in diameter, is left to 5 sons, 4 of whom get each what is equivalent to a circle 400 yards in diameter, while the fifth gets the remainder. If the area of a circle is $\frac{355}{452}$ of the square on the diameter, what per-centage of the estate goes to each son:
12. A person walks from Rugby to London in 4 days, and back in 5 days. Each day he walks one mile less than on the preceding day. What is the distance between the two places?

## No. 8.-GEOMETRY (II.).

## Lower Grade.

$$
\text { Monday, 18th June. } 12 \text { to } 2 \text { Р.м. }
$$

Give your working in full.
Endeavour rather to answer a moderate number of Questions accurately and fully than to answer a large number imperfectly.

1. If two triangles have three sides of the one respectively equal to three sides of the other, they are equal in every respect.

The triangles $A B C, A^{\prime} B^{\prime} C^{\prime}$ are right angled at $C$ and $C^{\prime}$. $C D$ and $C^{\prime} D^{\prime}$ are the perpendiculars from $C$ and $C^{\prime}$ on $A B$ and $A^{\prime} B^{\prime}$ respectively; if $B C=B^{\prime} C^{\prime}$ and $C D=C^{\prime} D^{\prime}$, shew that the triangles are equal in every respect.
2. The complements of the parallelograms about the diagonal of a parallelogram are equal to each other.

If two points be taken in the diagonal through which parallel lines are drawn to the sides, show that the two corner figures remote from the diagonal are equal.
3. In the triangles $A B C, A^{\prime} B^{\prime} C^{\prime}, A \dot{B}=A^{\prime} B^{\prime}, A C=A^{\prime} C^{\prime}$, and L. $A>$ $\angle A^{\prime}$, show that $B C>B^{\prime} C^{\prime}$.

If $D$ and $D^{\prime}$ be the middle points of $B C$ and $B^{\prime} C^{\prime}$, shew that $A D<A^{\prime} D^{\prime}$.
4. Shew that parallelograms on the same base and between the same parallels are equal in area. .

Deduce the ordinary rule for computing the area of a parallelogram.
5. Shew that the area of an equilateral triangle on the hypotenuse of a right-angled triangle is equal to the sum of the areas of the equilateral triangles on the sides.
6. $O$ is the middle point of $A B, D$ any other point whatever in $A B$, Show that the sum of the squares on $A D$ and $B D$ is double the sum of the squares on $O A$ and $O D$.

Given two points, $A$ and $B$, find a point $D$ in $A B$ such that $A D^{2}+B D^{2}-2 A D \cdot B D$ shall be equal to a given square.
7. Shew that the angle in a circular segment is less than, equal to, or greater than a right angle according as the segment is greater than, equal to, or less than a semicircle.
$A$ and $B$ are fixed points, $A L, B M$ two variable straight lines which are always parallel and like directed. $P A$ and $P B$ bisect the angles $L A B$ and $M B A$ respectively; find the locus of $P$.
8. When are two circles said to touch ?

If two circles touch, shew that the straight line through their centres passes through the point of contact?
$A L$ and $B M$ are parallel. The circle $C$ touches $A L$ and $A B$, its point of contact with the former being $P$. The circle $D$ touches $B M$ and $A B$, the former at $Q$. If the circles $C$ and $D$ touch other, show that $P Q$ passes through the point of contact.
9. If four points $A, B, C, D$ are in order on the same straight line, $A C \cdot B D=A B \cdot C D+B C \cdot A D$.
10. Three times the sum of the squares on the three sides of a triangle is equal to four times the sum of the squares on the three medians.
11. Show that the three circles which each go through two angles of a triangle and the intersection of its perpendiculars are each equal to the circumscribing circle of a triangle.
12. If any hexagon be inscribed in a circle, the sum of its first, third and fifth angles is equal to four right angles.

> No. 2.-GEOMETRY (I.).

## Higher Grade and Honours.

$$
\text { Monday, 18th June. } 12 \text { to } 2 \text { p,M. }
$$

Give your working in full.
Endeavour rather to answer a moderate number of Questions accurately and fully than to answer a large number imperfectly,

1. Prove that two right-angled triangles are equal in every respect when two sides of the one, or a side and an angle of the one, are respectively equal to the corresponding parts in the other. Indicate carefully the different fundamental propositions on which your demonstration rests.
$A B C, A^{\prime} B^{\prime} C^{\prime}$ are two triangles each right-angled at $A, A D^{\prime}$ and $A^{\prime} D^{\prime}$ are the perpendiculars from $A$ and $A^{\prime}$ on $B C$ and $B^{\prime} C$ respectively. If $B C=B^{\prime} C^{\prime}$ and $A D=A^{\prime} D^{\prime}$, show that the two triangles are equal in every respect.
2. Prove that the square on the hypotenuse of a right-angled triangle is equal to the sum of the squares on its sides.

In any acute-angled triangle $A B C$ squares are described externally on the sides, viz., $B L M C$ on $B C, C P Q A$ on $C A, A R S B$ on $A B$. $A D, B E, C F$ are perpendiculars on $L M, P Q, R S$ respectively. Prove that the following pairs of rectangles are equal : $A \mathscr{E}$ and $A F ; B F$ and $B D ; C D$ and $C E$.

What important theorem of Euclid's may be deduced from this result?
3. Prove (without assuming any theorem of a similar kind for the circle) that the rectangle under the segment of a chord through $P$ is equal to the difference between the squares of the radius of the circle and the distance of $P$ from the centre.

Point out the various important particular cases of this theorem.
$A$ and $B$ are two fixed points on a given straight line $L . \quad P$ is a point on a variable circle $C$ through $A$ and $B$ such that the part of the tangent to $C$ at $P$ intercepted between $P$ and the given line $L$ is of constant length : find the locus of $P$.
4. Prove that the bisectors of the external and internal angles of a triangle divide the base in the ratio of the sides.
$L$ is a given straight line, $A$ and $B$ two points on opposite sides of it: find a point $P$ in $L$ such that $L$ bisects the angle $A P B$.
5. Show how to inscribe a circle in any given equilateral and equiangular polygon, and prove that the same construction enables you to describe a circle about it.
6, If the diagonals of a quadrilateral cut each other at right angles, the four feet of the perpendiculars on the sides from the intersection of the diagonals are on the circumference of a circle.
7. On a given straight line describe a rectilineal figure similar to a given rectilineal figure, so that the given line may be homologous to an assigned side of the given figure.

If the given figure be a right-angled triangle, and each of its three sides be taken in turn as the assigned side, what would be the relation between the areas of the three figures thus described ?
8. If a triangle have 27,24 , and 7 as its sides, find (1) what sort of triangle it is, (2) what is the length of the perpendicular to any one of the sides, (3) what is the length of the radius of the inscribed circle.

## Optional Questions.

9. Prove the fundamental property of the radical axis of two circles; and deduce the existence of the radical centre.
$A B C D$ is a quadrilateral which can be circumscribed about a circle. The circle $E$ touches $D A$ in $P$ aud $A B$ in $Q$; the circle $F$ touches $A B$ in $Q$ and $B C$ in $R$; the circle $G$ touches $B C$ in $R$ and $C D$ in $S$; the circle $H$ touches $C D$ in $S$ and also touches

- 53069. 

$D A$. Show that the circles $E$ and $G$ and the circles $F$ and $H$ (if they intersect) intersect on points which lie on the diagonals of the quadrilateral.
10. If any straight line meet the sides of the triangle $A B C$ in the points $D, E, F$ respectively, shew that, with a certain convention as to algebraic sign, the product of the three ratios $A D: B D$, $B E: C \mathscr{E}, C F: A F$ is +1 ; and conversely.

If the tangents at $A B C$ to the circle circumscribed about the triangle $A B C$ meet the sides $B C, C A, A B$ in $D, E, F$ respectively, prove that $D, E, F$ are collinear.
11. Find the angles of a triangle with sides $27,24,7$; also of a triangle with sides $25,24,7$.
12. Prove that the volume of a pyramid is one-third the volume of a prism having the same base and the same altitude.

A solid is composed of a right circular cylinder surmounted by a right circular cone. The heights of the cone and cylinder are the same, viz., 3 feet; and they have a common radius, viz., 2 feet. Calculate to 2 places of decimals, the whole volume and the whole surface of the solid.

No. 9.-ALGEBRA (II.).

## Lower Grade.

Monday, 18th June. 3 p.m. to 5 P.M.
Give your working in full.
Endeavour rather to answer a moderate number of Questions accurately and fully than to answer a large number imperfcctly.

1. Expand and arrange according to powers of $x$

$$
\begin{aligned}
& (3 x-2)^{4} \\
& \text { (a) ; } \\
& (x-2)(x+2)\left(x^{2}+4\right)\left(x^{4}+16\right) \ldots \ldots(\beta) .
\end{aligned}
$$

Simplify-

$$
\frac{2 x^{4}+4 x^{3}-3 x^{2}+x+1}{x^{2}+3 x+1}
$$

2. Resolve the following into factors as far as you can :

$$
\begin{aligned}
& x^{2}+(a-b) x-a b \ldots \ldots . .(\alpha) ; \\
& (x-1)^{2}-(2 x-3)^{2} \ldots \ldots \ldots(\beta) ; \\
& 8 x^{3}+27 \ldots \ldots \ldots \ldots \ldots .(\gamma)
\end{aligned}
$$

3. Express each of the following as the simplest possible single fre tion:

$$
\begin{aligned}
& \frac{a+b}{a-b}-\frac{a^{2}+b^{2}}{a^{2}-b^{2}}+\frac{4 a^{2} b^{2}}{a^{4}-b^{4}} \cdots . .(a) \\
& \frac{x+1}{\frac{x+1}{x^{3}+1}+\frac{x-1}{x^{3}-1}} \underset{x+1}{x^{3}-1} \\
& x-1
\end{aligned} \cdots \ldots \ldots(B) .
$$

4. Solve the following equations:-

$$
\begin{aligned}
& \frac{a x+b}{a+b}+\frac{a x-b}{a-b}=2 \ldots \ldots \ldots(\alpha) \\
& \left.\begin{array}{l}
\frac{2}{3}(x+y)-5(x-y=1) \\
x+y=2(x-y)
\end{array}\right\} \ldots \ldots(\beta) .
\end{aligned}
$$

5. Find the two roots of the equation

$$
(x-1)(x-2)+(x-1)(x-3)+(x-1)(x-4)=0
$$

A certain sum of money, lent out for a number of years at 4 per cent., simple interest, amounted to $£ 280$. If the same sum had been lent out for twice as long at 5 per cent. simple interest, it would have amounted to $£ 400$; find the sum and the number of years.
6. Show that, if two integral functions of $x$ have any common factor, it will be a factor in their sum or difference; and exemplify the theorem.

Hence show that $x^{2}-x+1$ and $x^{2}+x+1$ have no factor in common.

Find the G.C.M. of

$$
x^{4}+2 x^{3}-2 x^{2}+2 x-3 \text { and } x^{4}-2 x^{3}-2 x^{2}-2 x-3
$$

7. Reduce to its simplest form $2 \sqrt{ } \overline{243}-\frac{7}{3} \sqrt{3}$.
8. If $x+y$ varies as $x-y$, show that $x^{2}+y^{2}$ varies as $x y$,
9. If $\frac{a}{b}=\frac{c}{d}=\frac{e}{f}, \& c$. , show that each of these fractions is equal to

$$
\frac{p a+q c+r e+\& \mathrm{c}}{p b+q d+r f+8 \mathrm{c}}
$$

where $p, q, r$, \&ce. are any numbers. Is there any restriction on $p, q, r, \& c$. in the case where negative values of $a, b, c, \& c$. are allowed?
10. Two men set out at the same time to walk, one from Glasgow to Inverness, 180 miles apart, at the rate of $m$ miles an hour, the other from Inverness to Glasgow, at the rate of $n$ miles per hour. Where will they meet?
11. Solve-
(1) $3 x^{2}=x+1$.
(2) $x^{2}-x+\frac{72}{x^{2}-x}=18$,
12. Find the cube root of

$$
x^{3}-9 x+\frac{27}{x}-\frac{27}{x^{3}}
$$

## No. 3.-ALGEBRA (I.).

## Higher Grade and Honours.

Monday, 18 th June. 3 p.m. to 5 p.m.

## Give your working in full.

Endeavour rather to answer a moderate number of Questions accurutely and fully than to answer a large number imperfectly.

1. Expand and arrange according to powers of $x$

$$
\left\{(b+c-a) x^{2}+(c+a-b) x+(a+b-c)\right\}\left\{x^{2}+x+1\right\}
$$

Expand, simplify and arrange symmetrically

$$
(b+c-a)^{2}(b-c)+(c+a-b)^{2}(c-a)+(a+b-c)^{2}(a-b)
$$

Find an integral function of $x$ of the first degree whose value is doubled when $x$ is doubled and which has the value 9 when $x=3$.
2. If $p \alpha^{3}+q \alpha^{2}+r \alpha+s=0$, prove from first principles that $p x^{3}+q x^{2}+$ $r x+s$ contains the factor $x-\alpha$.

Resolve the following into factors of the first degree:-

$$
\begin{aligned}
& 22 x^{2}+109 x+45 \ldots \ldots \ldots(\alpha) \\
& (x+1)^{3}+(2 x+1)^{3} \ldots \ldots \ldots(8) \\
& x^{3}+x y+x-y-2 \ldots \ldots(\gamma)
\end{aligned}
$$

3. What is meant by a proper algebraic fraction? Show that the sum of two proper algebraic fractions is alwnys a proper algebraic fraction.

$$
\begin{aligned}
& \text { Simplify } \frac{\left(x^{2}+x+1\right)^{2}-\left(x^{2}-x+1\right)_{2}}{\left(x^{2}+x+1\right)^{3}-\left(x^{2}-x+1\right)^{3}} \\
& \text { If } \frac{x^{3}+3 x}{\left(x^{2}-1\right)^{2}}=\frac{A x+B}{(x+1)^{2}}+\frac{C x+D}{(x-1)^{2}} \text {, where } A, B, C, D, \text { are mere }
\end{aligned}
$$ numbers, determine the values of $A, B, C, D$.

4. Explain carefully what is meant by a solution of a conditional equation involving one or more variables.

Show that, if all the solutions of $A x+B y+C=0$ be also solutions of $A^{\prime} x+B^{\prime} y+\mathrm{C}^{\prime}=0$, then, in general $A / A^{\prime}=B / B^{\prime}=C / C^{\prime}$.

Find as many solutions as you can of the following :-

5. If three simultaneous equations, $a x+b y+c z=0$,

$$
\begin{aligned}
& a^{\prime} x+b^{\prime} y+c^{\prime} z=0 \\
& a^{\prime \prime} x+b^{\prime \prime} y+c^{\prime \prime} z=0
\end{aligned}
$$

are consistent with any simultaneous values of $x, y, z$, except zeroes, find the relation that must exist between the constants.
6. Snive $(x+a)(y+b)=c^{2},(y+b)(z+c)=a^{2},(z+c)(x+a=) b$
7. Reduce to their simplest expressions :
8. If $\alpha$ and $\beta$ be the roots of the quadratic equation $x^{2}+p x+q=0$, find the equation whose roots are $\alpha(\alpha-\beta), \beta(\beta-\alpha)$.

Discuss, by drawing a curve or otherwise, the variation in the value of $\left(x^{2}-x+1\right) /(x-1)^{2}$ when $x$ varies from $-\infty$ to $+\infty$; and find whether this function has a maximum or a minimum value.

## Optional Questions.

9. Find the number of permutations of $n$ things taken $r$ at a time, 1st, when each thing may be repeated as often as we please ; 2 nd , when there is no repetition,

In how many different ways can sixteen school girls pair themselves for a walk so that one of the eight elder girls always walks with one of the eight younger ones? No attention is to be paid to the order of the pairs in the procession.
10. Show that the co-efficient of $x^{n}$ in the expansion of $(1+x)^{2 n}$ is double the co-efficient of $x^{n}$ in the expansion of $(1+x)^{2}{ }_{n}{ }^{-1}$.
11. The equation
$x^{3}+3 x^{2}+m x-13=0$ has $-2+3 i$ for a root (where $i^{2}=-1$ ), what are the other roots and what is the value of $m$ ?
12. The sides of a triangle being 107 and 119 , and the included angle $50^{\circ} 6^{\prime}$, find the other angles and the third side.
13. State, without proof, the formulae for expanding $\sin (A+B)$ and $\cos (A+B)$ in terms of the sines and cosines of $A$ and $B$; and deduce an expression for $\tan 3 A$ in terms of $\tan A$.

Prove that

$$
\cot ^{2} \frac{A}{2}+\tan ^{2} \frac{A}{2}-2=\frac{4}{1-2 \tan A \cot 2 A} .
$$

14. If $R$ be the radius of the circle circumscribing the triangle $A B C$, express $R$ in terms of $b, c$ and $A$.

Shew that
a $\cos A+b \cos B+c \cos C=4 R \sin A \sin B \sin C$.

## No. 4.-GEOMETRICAL CONICS.

Monday, 25 th June. 10 A.m. to 12 A. M.
Give your working in full.
Endeavour rather to answer a moderate number of questions accurately and fully than to answer a large number imperfectly.

1. Define a parabola, a tangent, a normal.

Prove that any tangent to a parabola bisects the angle between the line drawn from the focus to the point of contact and the perpendicular from that point on the directrix.
2. If $S$ be the focus of a parabola, A the vertex, and PN the perpendicular drawn from P , a point in the parabola, to AN the axis, prove that $\mathrm{PN}^{2}=4 \mathrm{AS} \cdot \mathrm{AN}$.

If SP be bisected in $Q$, show that the locus of $Q$ is a parabola. Determine its vertex and latus rectum.
3. If the tangent to a parabola at P meet the axis in T , then $\mathrm{NT}=2 \mathrm{AN}$.
If PN be produced to meet the parabola again in Q , show that the centre of the circle described about the triangle PQT is the same for all positions of P .
4. The tangents at the extremities of a focal chord of a parabola intersect at right angles in the directrix.
$P Q$ is a focal chord, and the tangents at its extremities meet in R. Proves that $\mathrm{RP}^{2}: \mathrm{RQ}^{2}=\mathrm{SP}: \mathrm{SQ}$.
5. Define an ellipse both from its focus and directrix property, and from the property of its two focal distances.

Assuming one of these definitions, show how the other may be derived from it.
6. If C be the centre of an ellipse, and the tangent at a point P meet the axis-major $\mathrm{AA}^{\prime}$ in T , and N be the foot of the perpendicular drawn from ${ }^{P}$ to the axis, then $\mathrm{CT} \cdot \mathrm{CN}=\mathrm{CA}^{2}$.
7. From S and H, the foci of an ellipse, SY and HZ are drawn perpendicular to the tangent. Prove that $\mathrm{SY} \cdot \mathrm{HZ}=\mathrm{CB}^{2}$. Show that SZ and HY intersect on the normal.
8. The area of the parallelogram formed by drawing tangents to an ellipse at the extremity of a pair of conjugate diumeters is equal to the rectangle contained by the axes of the ellipse.
The normal at P meets the axis-minor in Q . Show that a circle may be described through the points PSQH .

## Optional Questions.

9. The section of a cone made by a plane touching a given sphere about which the cone is circumscribed is a parabola, ellipse, or hyperbola, of which the point of contact is a focus.
Show that in each of the two latter cases the given plane touches a second inscribed sphere at a second focus.
10. The rectangle contained by the perpendiculars drawn from any point in a hyperbola to the asymptotes is constant.
Having given the asymptotes of an hyperbola and one point in the curve, find the vertex.
11. Show that in any conic section, if the tangent at P meet the directrix in R the angle PSR is a right angle.

If PS be produced to meet the conic in Q , and the directrix in $T$, prove that $\mathrm{SP}: \mathrm{SQ}=\mathrm{PT}: \mathrm{QT}$.
12. Give mechanical methods of describing the parabola, the ellipse, and the hyperbola.

> No. 5.-ANALYTICAL GEOMETRY.
> Monday, 25th June. 12.30 to 2.30 P.M.

Give your working in full.
Endeavour rather to answer a moderate number of questions accurately and fully than to answer a large number imperfectly.

1. Explain how the position of a point in a plane is determined by rectangular coordinates.

Find the length of the line joining the points whose coordinates are $(2,2)$ and $(-2,-1)$.
2. Show that the equation $2 x+3 y=5$ represents a straight line, and find the points where it cuts the coordinate axes.
3. Find the equation to the straight line mentioned in the first question and reduce it to the form $y=m x+c$. What do $m$ and $c$ represent?
4. Find the tangent of the angle between the lines

$$
\begin{gathered}
\mathrm{A} x+\mathrm{B} y+\mathrm{C}=0 \\
\mathrm{~A}^{\prime} x+\mathrm{B}^{\prime} y+\mathrm{C}^{\prime}=0
\end{gathered}
$$

What is the condition that these lines be at right angles?
5. Find the length of the perpendicular drawn from the point $x^{\prime} y^{\prime}$ to the line $\mathrm{A} x+\mathrm{B} y+\mathrm{C}=0$.
6. Find the area of the triangle contained by the straight lines

$$
\begin{gathered}
x+2 y=5, \\
2 x+y=7, \\
y-x=1 ;
\end{gathered}
$$

and draw the figure.
7. Show that the lines

$$
\begin{aligned}
& 2 y=3 x+4, \\
& 4 y=4 x+3, \\
& 6 y=5 x+2
\end{aligned}
$$

meet in a point.
8. If the distance of a point from the origin bear a fixed ratio to its distance from the axis of $x$, find its locus.

## Optional Questions.

9. Show that the equation

$$
x^{2}+y^{2}+a x+b y+c=0
$$

represents a circle. Find its centre and radius.
If this circle passes through the points $(2,0),(0,2)$, and $(2,2)$, find $a, b$, and $c$.
10. If $r$ and $\theta$ be the polar coordinates of a point, determine what loci are represented by the equations
(1) $r=c$,
(2) $r \sin \theta=c$,
(3) $r \sin (\theta-\alpha)=c$.
11. If $y^{2}=4 a x$ be the equation to a parabola and $(h, k)$ be a point on the curve, find the equations to the tangent and normal at that point.
12. If $a, \beta$, and $\gamma$ be the perpendicular distances of a point P from the sides of a triangle, investigate the meaning of the equations $\alpha-\beta=0, \beta-\gamma=0, \gamma-\alpha=0, \alpha+\beta=0, \alpha+\beta+\gamma=0$.

## No. 6.-DYNAMICS.

$$
\text { Monday, 25th June. } 3 \text { р.м. to } 5 \text { р.м. }
$$

Give your working in full.
Endeavour rather to answer a moderate number of questions accurately and fully than to answer a large number imperfectly.

1. Define Velocity. How is Uniform Velocity measured ?

Two men ride along two roads at right angles, at the rates of five miles an hour and 12 miles an hour. Find the velocity of one relatively to the other.
2. A body falls from rest with uniform acceleration $g$. Find the equations of motion.

If $g=32 \cdot 2$, find the length moved in $4 \frac{1}{2}$ seconds.
3. State Newton's three Laws of Motion.
4. Forces acting at a point are represented in magnitude and direction by three sides of a quadrilateral figure taken in order. Find their resultant. Show whether your proof holds good if the angular points are not all in one plane.
5. Find the resultant of two parallel forces acting in similar directions at two points of a rigid body.

A rod, two feet long, weighs one pound, and has masses of one and three pounds hanging from its extremities. Where must it be supported so as to balance?
6. Define Centre of Gravity, and find that of a parallelogram.

What other names have been given to the Centre of Gravity ?
Part of a parallelogram is cut off by joining the middle points of two adjucent sides. Find the centre of gravity of the remainder.
7. Describe one form of steel-yard.
8. A mass of one ton rests on a smooth plane which rises 2 in 5. What horizontal force is required to keep the mass from slipping?

Optional Questions.
9. Define work. How is it measured ?

How much work is done by a man of 12 stone (1) in climbing a hill 800 feet high, (2) in walking a mile along a level road ? What considerations are neglected in your calculation?
10. Give the laws of Statical Friction.

What is the Angle of Repose? Give any instance of its occurrence in Nature.

## 11. Define a liquid.

Prove that the surface of a liquid at rest is horizontal.
12. A body A, weighing one pound, is found to float with half its volume under water. It is then attached to a body B, weighing two pounds, and the combined mass is found to float with $\frac{7}{8}$ ths of its volume under water. Find the specific gravity (1) of A, (2) of B.

## DIFFERENTIAL CALCULUS.

$$
\text { Tuesday, 26th June. } 10 \text { A.m. to } 12 \text { A.M. }
$$

Give your working in full.
Endeavour rather to answer a moderate number of Questions accurately and fully than to answer a large number imperfectly.

1. When is one quantity said to be a function of another ?

Define a differential coefficient, and prove that, if $y$ be a function of $x$, and $x$ be a function of $t, \frac{d y}{d t}=\frac{d y}{d x} \times \frac{d x}{d t}$.
2. Find $\frac{d y}{d x}, \frac{d^{2} y}{d x^{2}}$, and $\frac{d^{3} y}{d x^{3}}$ in each of the following cases :-
(1.) $y=(x+a)^{3}$,
(2.) $y=a^{x}$,
(3.) $y=\sin x+\cos x$.
3. Obtain the differential coefficients of the following functions :-

$$
y=\frac{1-x}{\sqrt{1+x^{2}}}, \quad y=\cos ^{-1} \frac{b+a \cos x}{a+b \cos x}
$$

4. State and prove Leibnitz's Theorem for the differentiation of a product of two functions.

$$
\text { Find } \frac{d^{4} x^{2} \cos x}{d x^{4}}
$$

5. Enunciate Taylor's Theorem.

Deduce Maclaurin's Theorem, and apply it to expand $\sin x$ in ascending powers of $x$.
6. If $\frac{f(x)}{\phi(x)}$ be a fraction such that both numerator and denominator vanish when $x=a$, find the limit to which the fraction tends as $x$ approaches the value $a$.

Find the limiting values of
(1.) $\frac{2-7 x+8 x^{2}-3 x^{3}}{3-8 x+7 x^{2}-2 x^{3}}$ when $x=1$.
(2.) $\frac{1-x^{2}}{2 x} \log \frac{1+x}{1-x}$ when $x=0$.
7. If the equation to a curve be of the form

$$
u=f(x, y)=0
$$

show that

$$
(\mathrm{X}-x) \frac{d u}{d x}+(\mathrm{Y}-y) \frac{d u}{d y}=0
$$

s the equation to the tangent at the point $(x, y)$.
Find the equations to the tangent and normal at any point in the curve $\frac{x^{2}}{a^{2}}-\frac{y^{2}}{b^{2}}=1$.
8. Define a pedal curve.

Show that the equation to the parabola

$$
y^{2}-4 a x=4 a^{2}
$$

may be put into the form $p^{2}=a r$, and deduce the equation to its pedal curve.


